

Variable-Resolution Multi-Physics Modeling of the Upper Colorado River Basin

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New Thinking

In cooperation with:

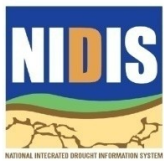
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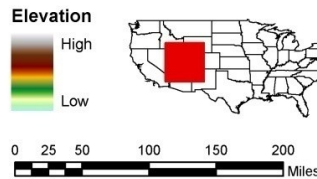
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Upper Colorado River Basin



- States
- Dams
- Streams
- Reservoirs
- Upper Basin
- Lower Basin



Basin Area: 288,000 km²

Streams: 467,000 km

Population: 900,000
(USBR)

Area above 2700 m: 14.5%
(9,000 ft)

Area above 3050 m: 3.2%
(10,000 ft)

High Altitude Complexity



Law of the River, Colorado River Compact, 1922

Lees Ferry, AZ, is the legal
dividing point between
Upper and Lower Basin

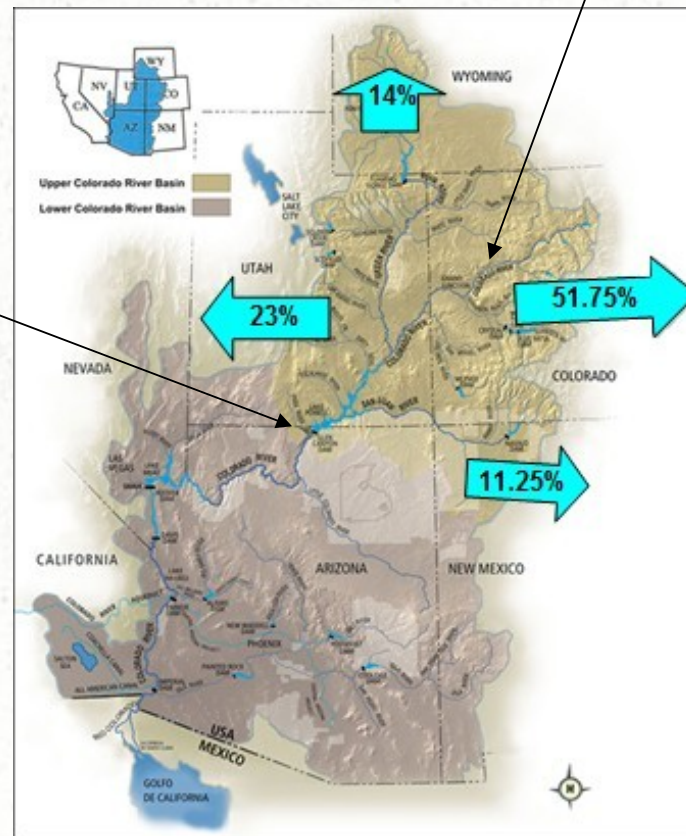
Lower Basin (CA, AZ, NV)
guaranteed 7.5 MAF/y

plus

Mexico- 1.5 MAF/y

Note: 1 AF = 1.233 MI

Upper Basin (CO, UT, WY, NM),

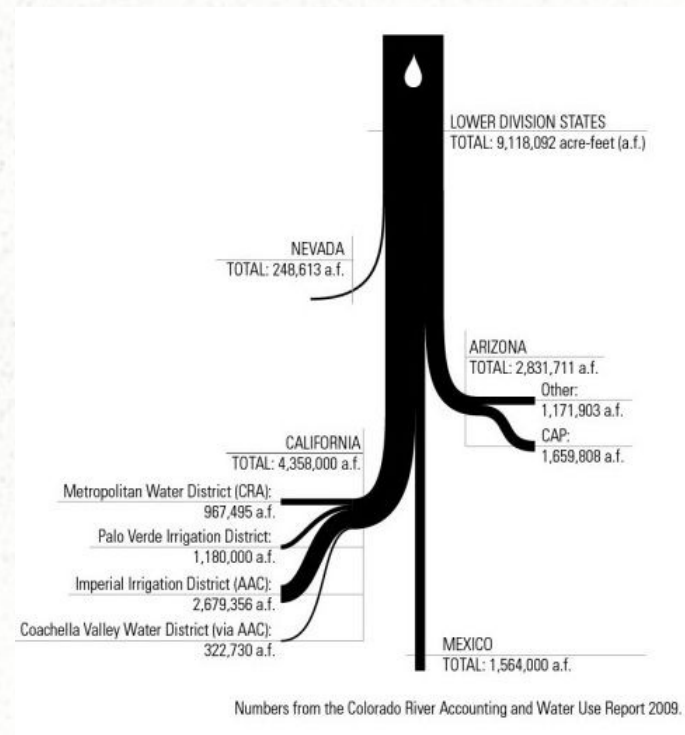
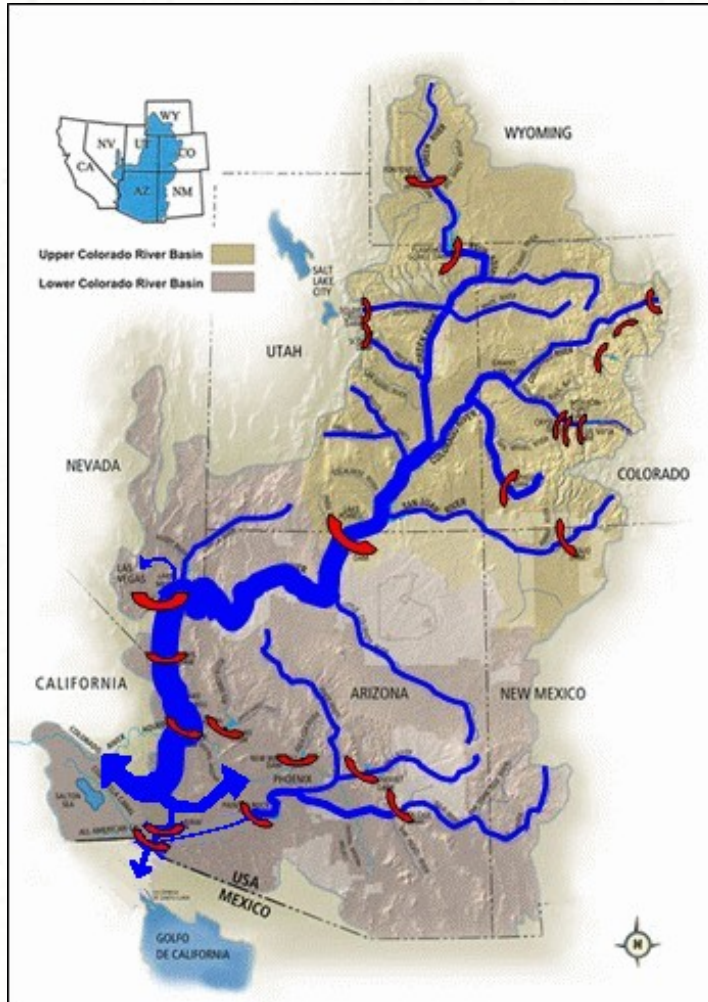


Glen Canyon Dam: The Upper States' bank account

- Pre-1963 average 12,963,000 AF
- Post-1963 average 10,701,000 AF



Colorado River Basin



A big watershed problem:

- Upper Colorado River Basin: 280,000 km²
- High resolution important in mountains, where slope, aspect, vegetation, wind, drive snow redistribution, sublimation, and melt.
- Low resolution in broad and extensive basins, where runoff is infrequently produced.



CI-WATER Component 3 Objective

Develop a high-resolution, large-scale hydrologic model to answer three questions:

- What are the potential impacts of climate change on the long-term yield of water from the upper Colorado River basin?
- How will future land-use changes due to development and natural causes such as fire, pine bark beetle affect water supplies?
- What are the effects of trans-basin diversions and increases in water consumptive use on the water storage in Lake Powell in 30-50 years?

Table 1. State **Population** Growth as Dramatic as Municipal Growth

State	1900	1950	1990	2000	2007
Colorado	539,700	1,325,089	3,294,394	4,301,261	4,861,515
Arizona	122,931	749,587	3,665,228	5,130,632	6,338,755
California	1,485,053	10,586,223	29,760,021	33,871,648	36,553,217
Utah	276,749	688,862	1,722,850	2,233,169	2,645,330
Nevada	42,335	160,083	1,201,833	1,998,257	2,565,382
New Mexico	195,310	681,187	1,515,069	1,819,046	2,499,481
Wyoming	92,531	290,529	453,588	493,782	532,668

Source: U.S. Census Bureau.

Fire and
land use
changes:



Snowfall and
redistribution:

Research Goals

- Increase accessibility of high performance Petascale computing to water resources researchers, engineers, and managers.
- Produce a set of modeling tools that allow consideration of future conditions in a modeling and probabilistic framework.
- Engage the wider community by releasing the code developed for research, development, and testing.

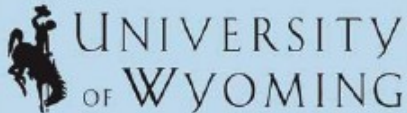
Petascale??

- HPC hydrologic modeling is in its infancy.
- We seldom do terascale modeling!
- We often do single CPU gigascale modeling.
- High Performance Computing is a new frontier for hydrologic modeling.

The NCAR-Wyoming Supercomputing Center (NWSC) provides dedicated *petascale* capabilities for geosciences.



NWSC Partners:



Architects, Contractors and Consultants:

H+L Architecture | Saunders Construction, Inc. | California Data Center Design Group | Rumsey Engineers | RMH Group
Martin & Martin Consulting Engineers | Rider Levett Bucknall | Reliable Resources | E Cube, Inc.

Wyoming's 20% Share of NWSC's **72,300** cores represents a huge increase in EPSCoR HPC capabilities...

- On the latest (6/11) Top500 list of fastest supercomputers, Wyoming's share on NWSC-1 alone is estimated to be...
 - The 28th fastest computer in the world
 - The 14th largest supercomputer in the US
 - The largest system in an EPSCoR state outside of Department of Energy facilities
 - The largest resource controlled by a university in the US

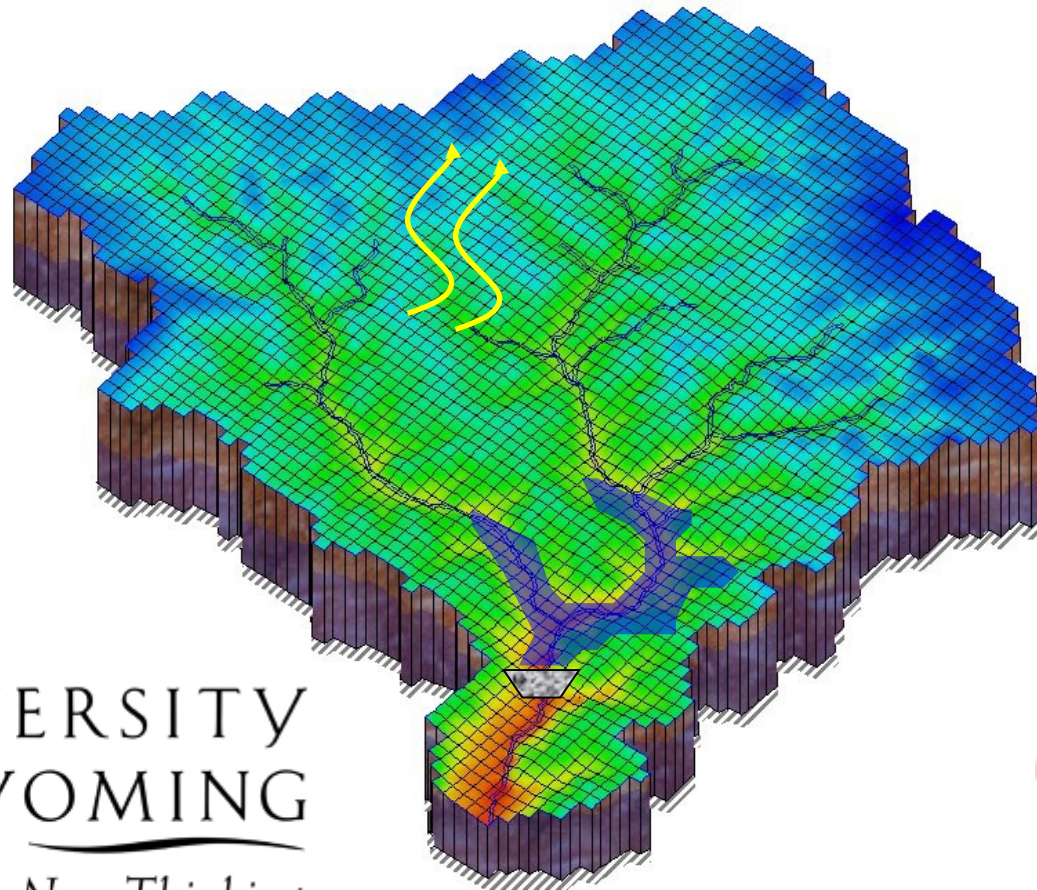
Reference: <http://www.top500.org>

Our Collaborators

- U.S. Army Corps of Engineers, Engineer Research and Development Center, Vicksburg, Mississippi, Coastal & Hydraulics and Information Technology Laboratories
- National Center for Atmospheric Research, Research Applications Laboratory



Gridded Surface/Subsurface Hydrologic Analysis (GSSHA) model



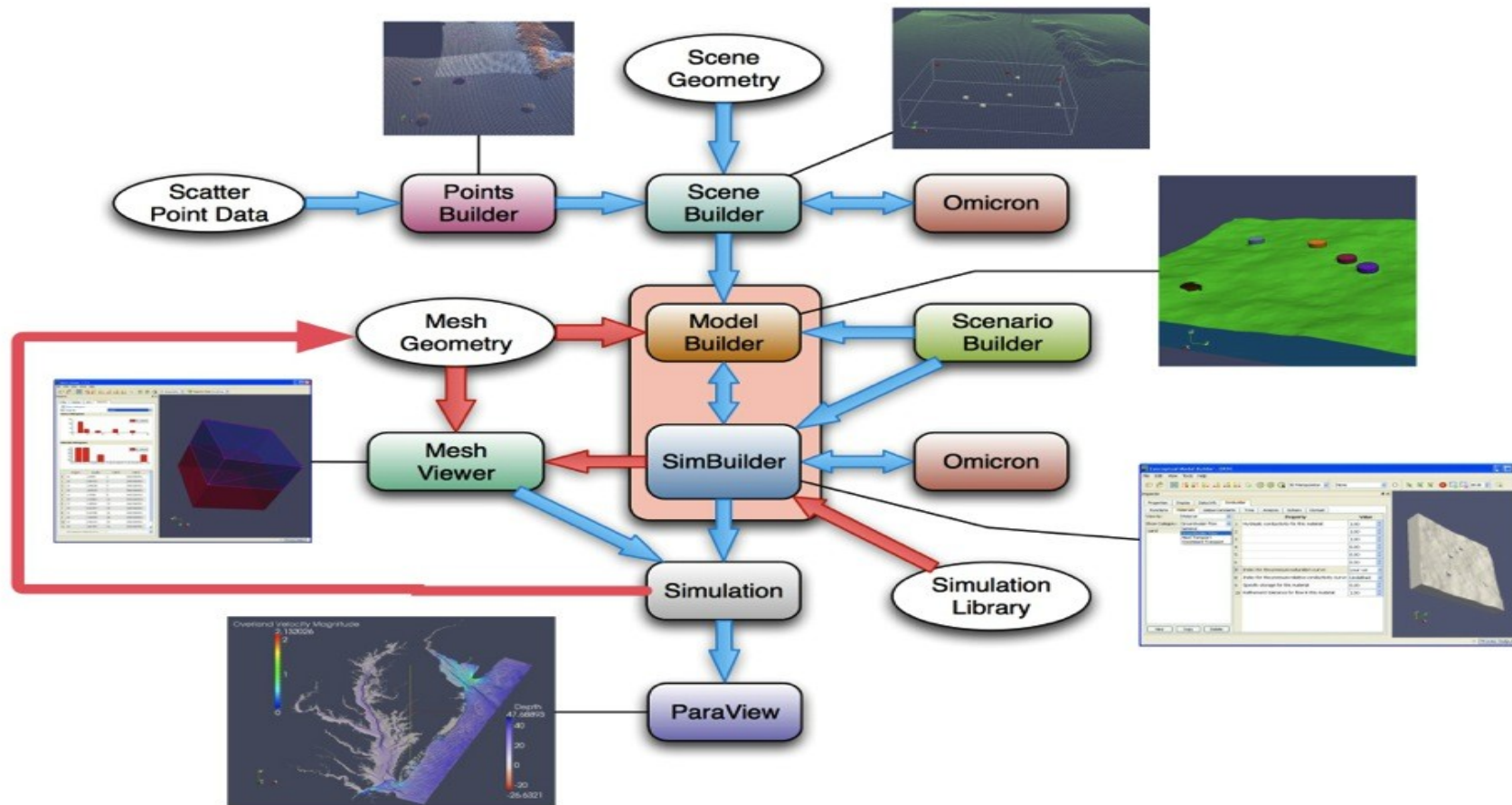
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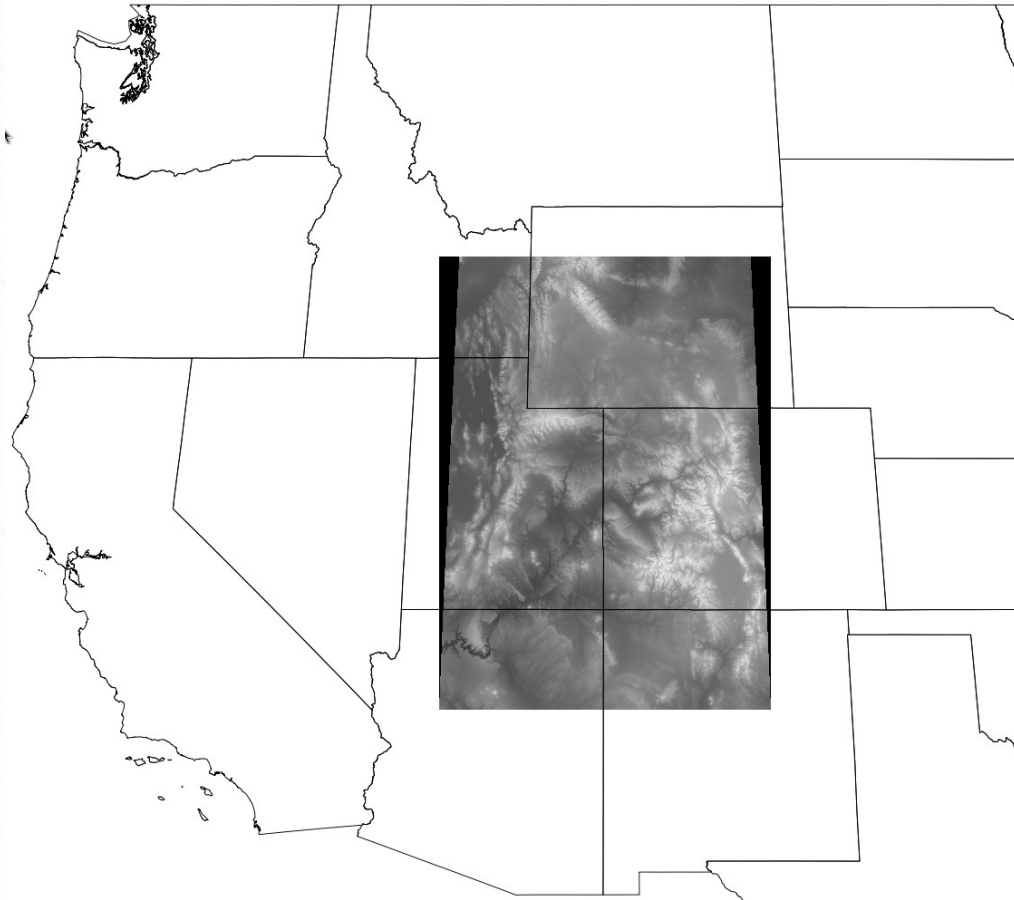
GSSHA

- Square grid (5 to 90 m typical)
- Multi-solver: different approximations of full PDE's, finite-difference and finite-volume.
- Multi-physics: different PDE's, or hybrid equations (mixed overland/groundwater)
- 2D overland flow and groundwater flow
- 1D channel routing with hydraulic structures
- Richards or Green-Ampt Redistribution coupling between overland flow and groundwater
- Erosion/deposition and sediment transport

Computational Model Builder Work Flow

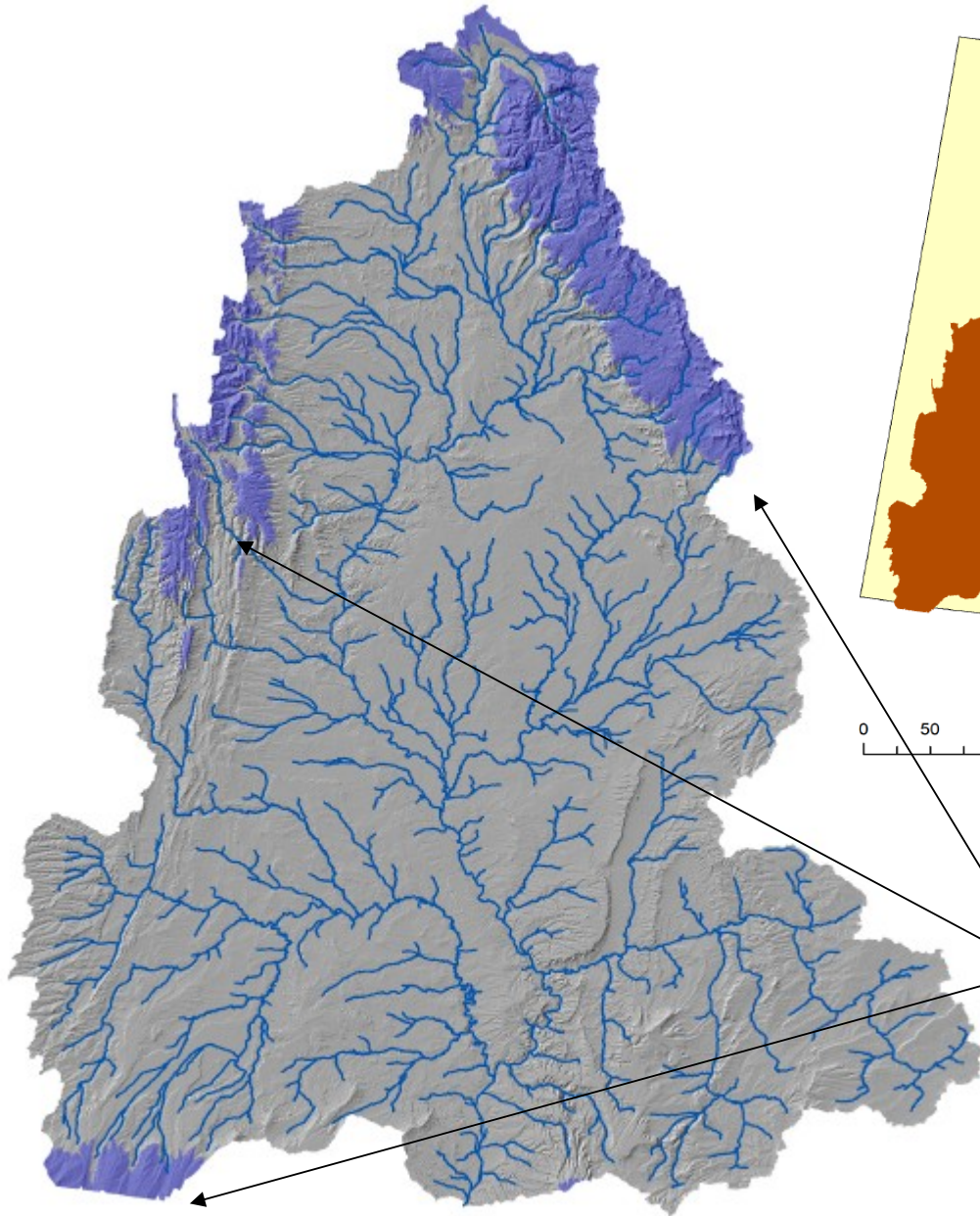


Interrupted Sinusoidal Projection



- Preserves area perfectly
- Lines of latitude are horizontal lines
- Longitudes converge towards the pole
- Can describe Amazon basin with minimal distortion
- Inset shows 10 m Digital Elevation Model (32 GB)

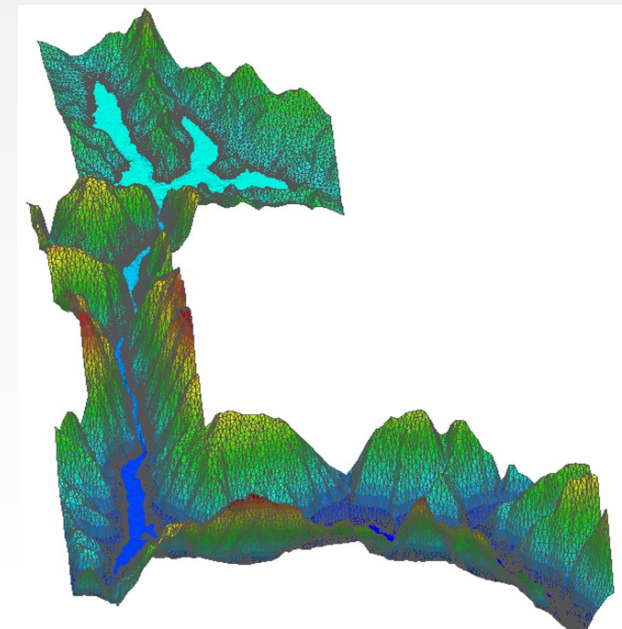
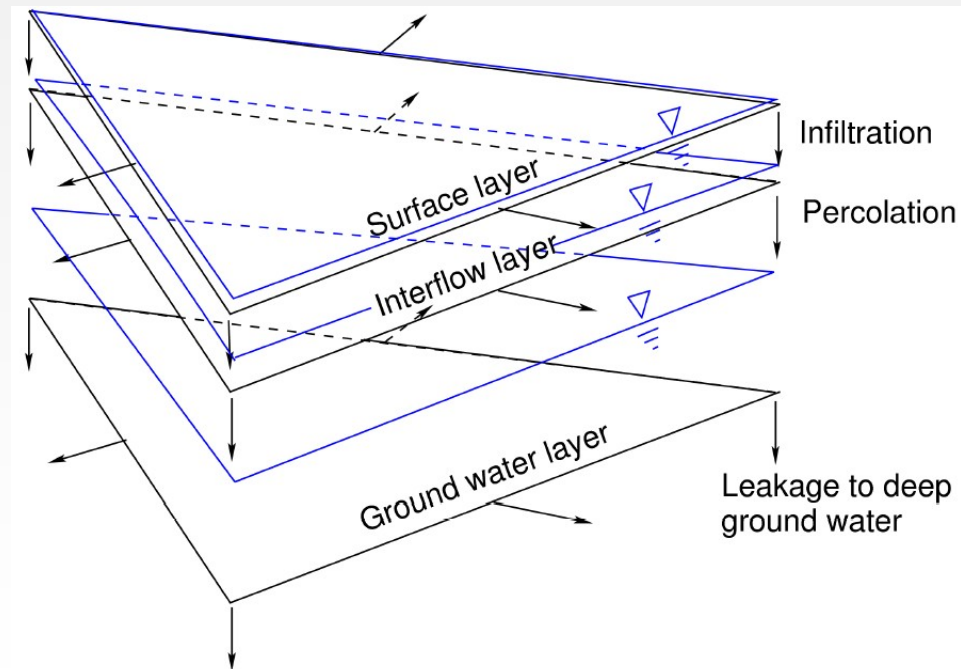
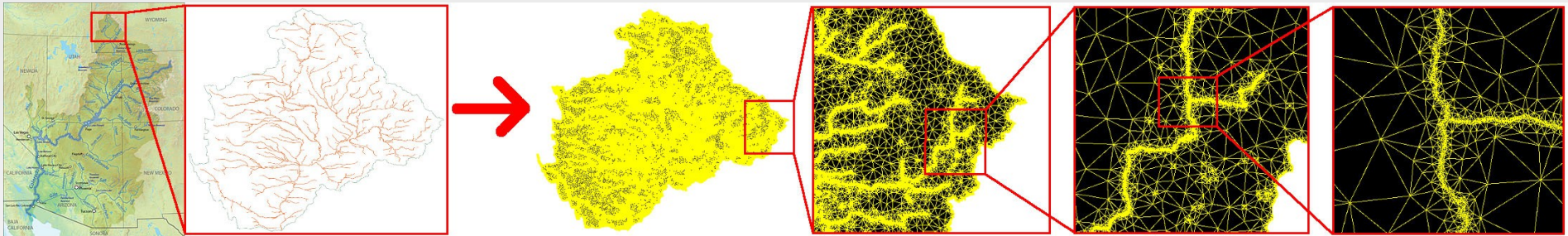
Test Area: Green River Basin in Wyoming



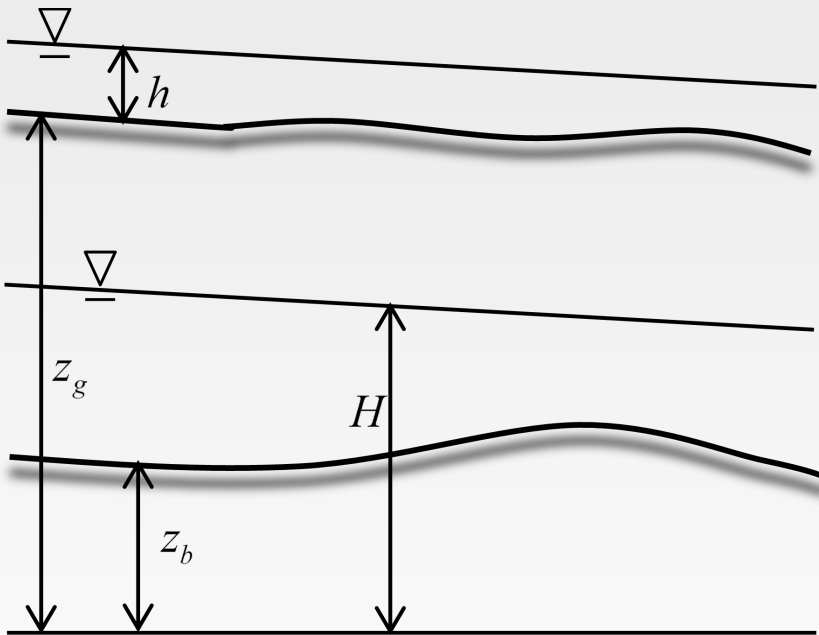
Darker blue areas are those above 2700 m elevation (9000 ft) where most snow melt occurs.



Variable Resolution Large Watershed Model



Mathematical model



surface water:
2D shallow water equations
dynamic wave
diffusive wave
kinematic wave

subsurface water:
3D Richards' equation

1D vadose zone flow
2D saturated groundwater flow

Mathematical model

2D dynamic wave:

$$\frac{\partial h}{\partial t} + \frac{\partial hu}{\partial x} + \frac{\partial hv}{\partial y} = 0$$

(hyperbolic convective)

$$\frac{\partial hu}{\partial t} + \frac{\partial huu}{\partial x} + \frac{\partial huv}{\partial y} = -gh \frac{\partial z}{\partial x} - \frac{gn_x^2 u \sqrt{u^2 + v^2}}{h^{1/3}}$$

$$\frac{\partial hv}{\partial t} + \frac{\partial huv}{\partial x} + \frac{\partial hvv}{\partial y} = -gh \frac{\partial z}{\partial y} - \frac{gn_y^2 v \sqrt{u^2 + v^2}}{h^{1/3}}$$

1D vadose zone flow

(ODE)

$$\frac{dZ_j}{dt} = \frac{K(\theta_d) - K(\theta_i)}{(\theta_d - \theta_i)} \left(\frac{\psi(\theta_d)}{Z_j} + 1 \right)$$

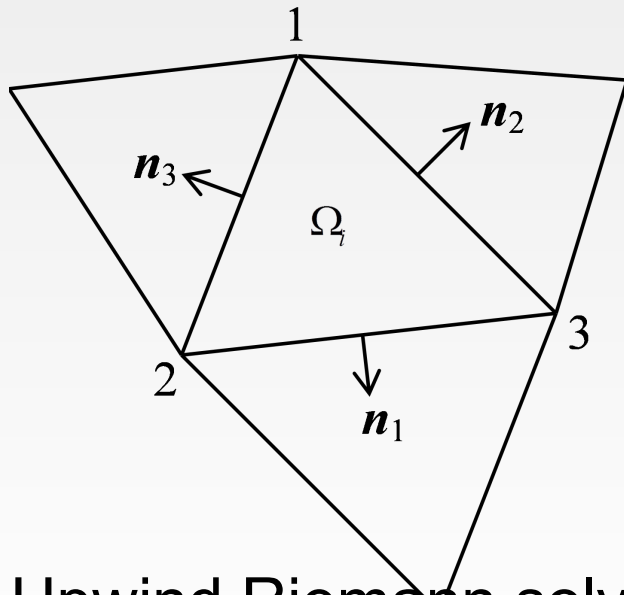
2D groundwater flow

(parabolic diffusive)

$$S_y \frac{\partial H}{\partial t} = \frac{\partial}{\partial x} \left(K_x (H - z_b) \frac{\partial H}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_y (H - z_b) \frac{\partial H}{\partial y} \right) + R$$

Numerical model

2D unstructured finite volume method for overland flow and saturated groundwater flow



$$\frac{\partial U}{\partial t} + \nabla \cdot F = S$$

$$\int \frac{\partial U}{\partial t} d\Omega + \int \nabla \cdot F d\Omega = \int S d\Omega$$

$$\int \frac{\partial U}{\partial t} d\Omega + \oint F \cdot n d\Gamma = \int S d\Omega$$

$$\frac{U_i^{n+1} - U_i^n}{\Delta t} + \frac{1}{\Omega_i} \sum_{j=1}^3 F_{ij} \cdot n_{ij} \Delta\Gamma_{ij} = S_i$$

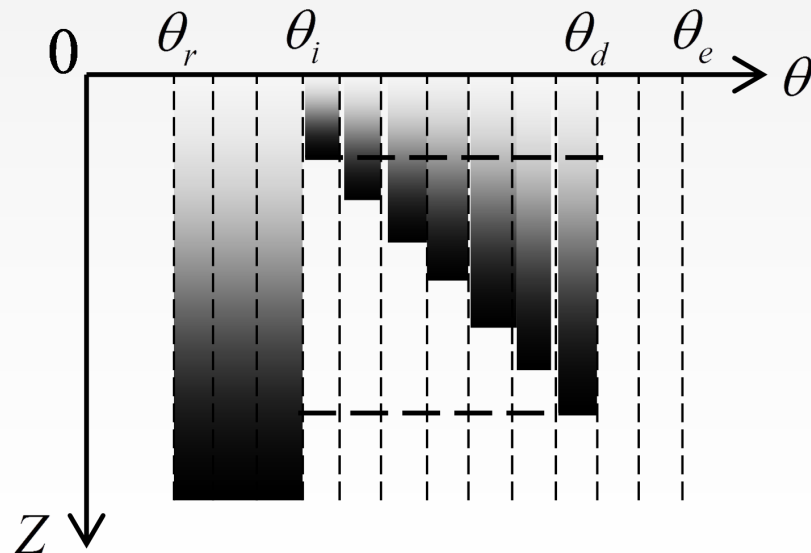
Upwind Riemann solver for convective flux in overland flow

Central difference for diffusion term in groundwater equation

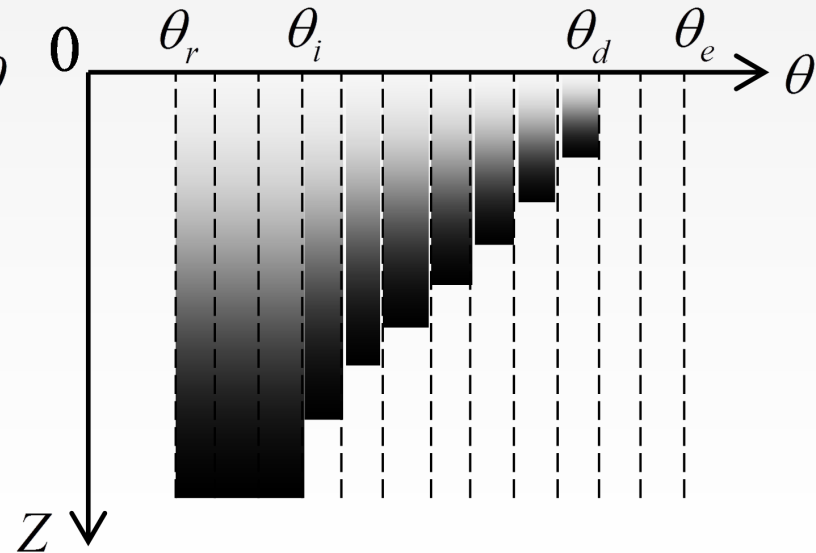
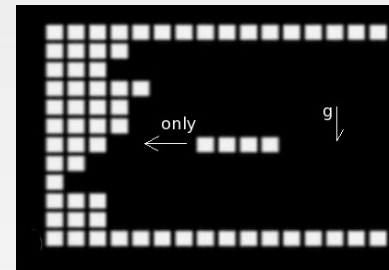
1-D Unsaturated Flow model: T-O (Talbot and Ogden, 2008) infiltration and redistribution method

Infiltration:

$$\frac{dZ_j}{dt} = \frac{K(\theta_d - K(\theta_i))}{(\theta_d - \theta_i)} \left(\frac{\Psi(\theta_d)}{Z_j} + 1 \right)$$



Redistribution:



Talbot and Ogden 1-D Infiltration (2008)

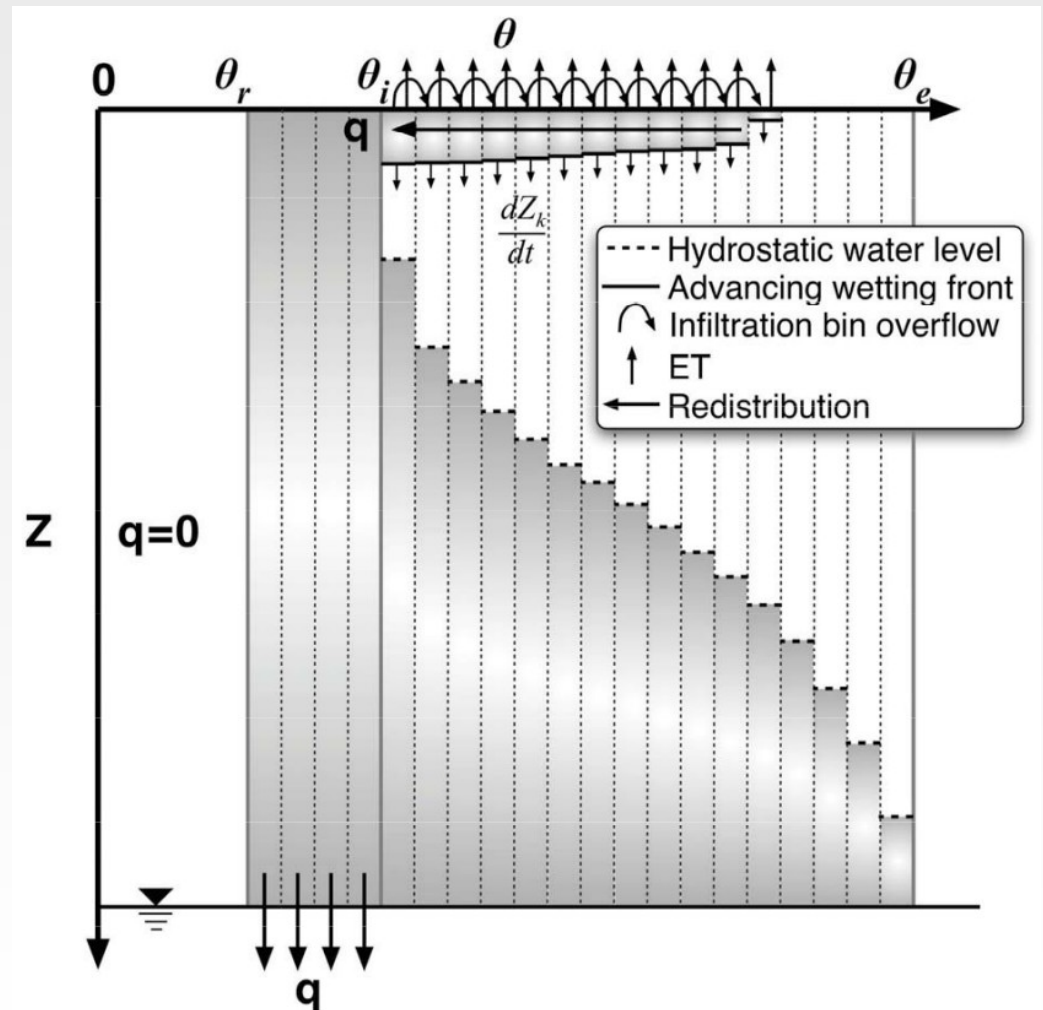
- No need to solve Richards (1931) equation:

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left(K(\theta) \frac{\partial \psi(\theta)}{\partial z} + 1 \right)$$

with:
$$\theta = \theta_r + \frac{\theta_e - \theta_r}{\left(1 + \left(\alpha \frac{\psi}{\rho_w g} \right)^n \right)^m}$$

$$K(\theta) = \theta^{1/2} \left(1 - (1 - \theta^{1/m})^m \right)$$

$$m = 1 - 1/n \quad \Theta = \frac{\theta - \theta_r}{\theta_e - \theta_r}$$

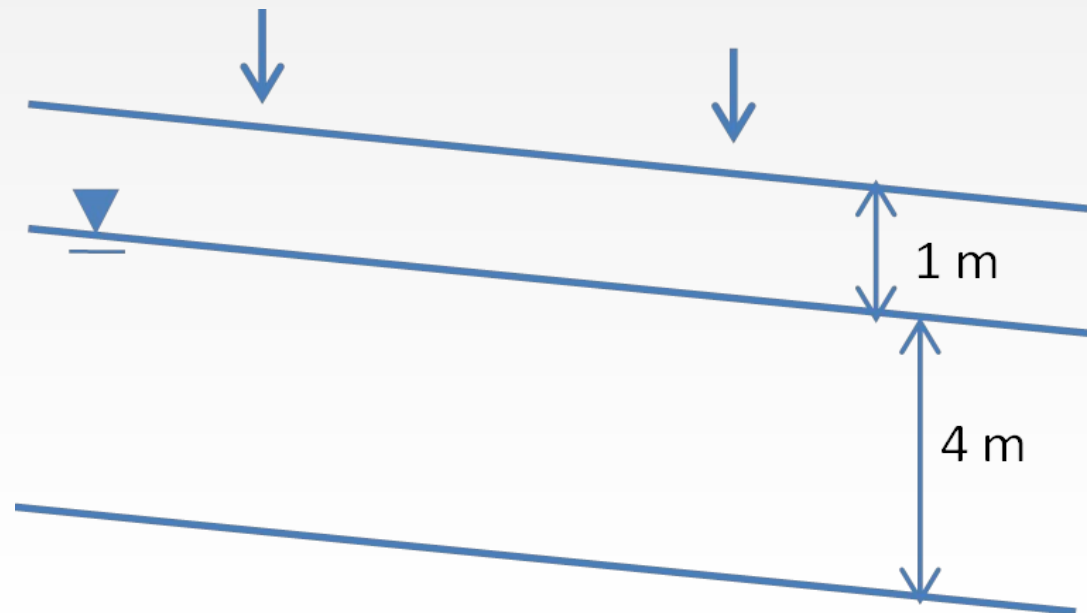


Numerical results: Hypothetical sloping plane (Sulis et al., 2010)

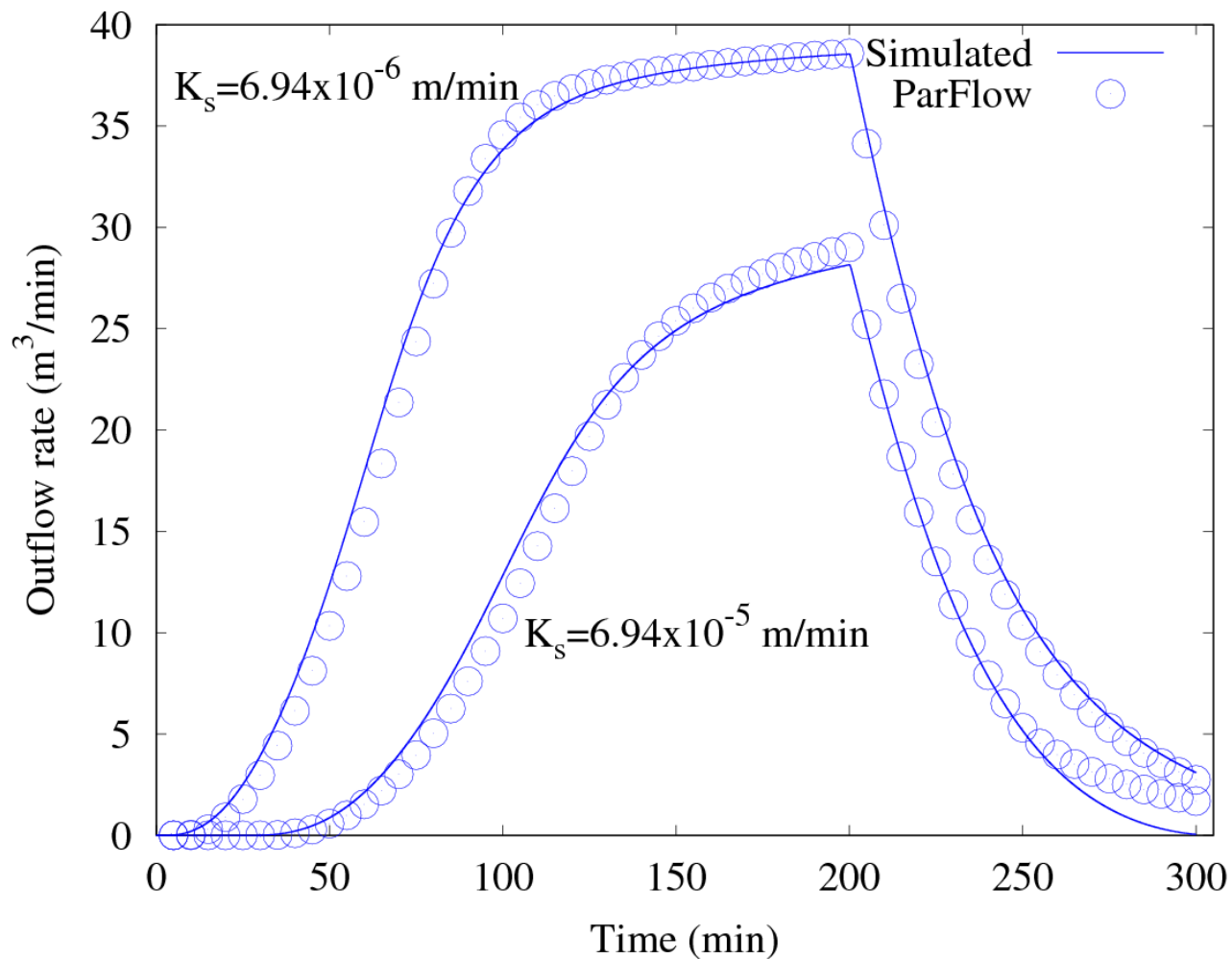
400 m X 320 M sloping plane;

5 m deep soil with water table 1 m below;

Uniform rainfall intensity of 33 mm/min for 200 minutes;



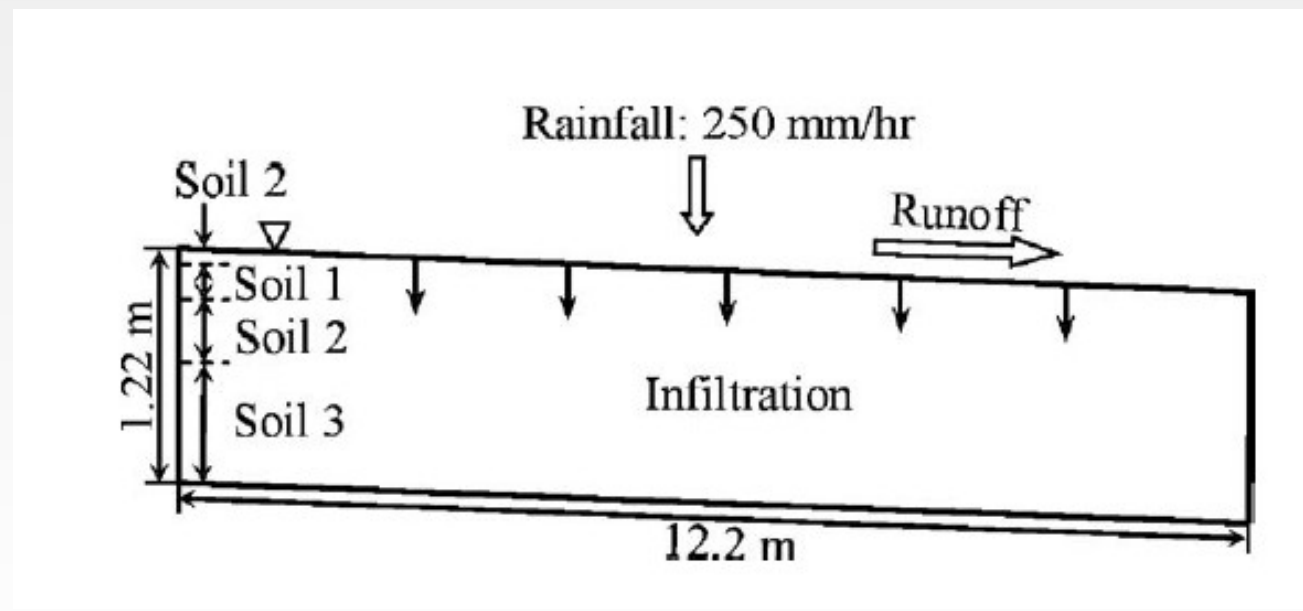
Numerical results: Hypothetical sloping plane (Sulis et al., 2010)



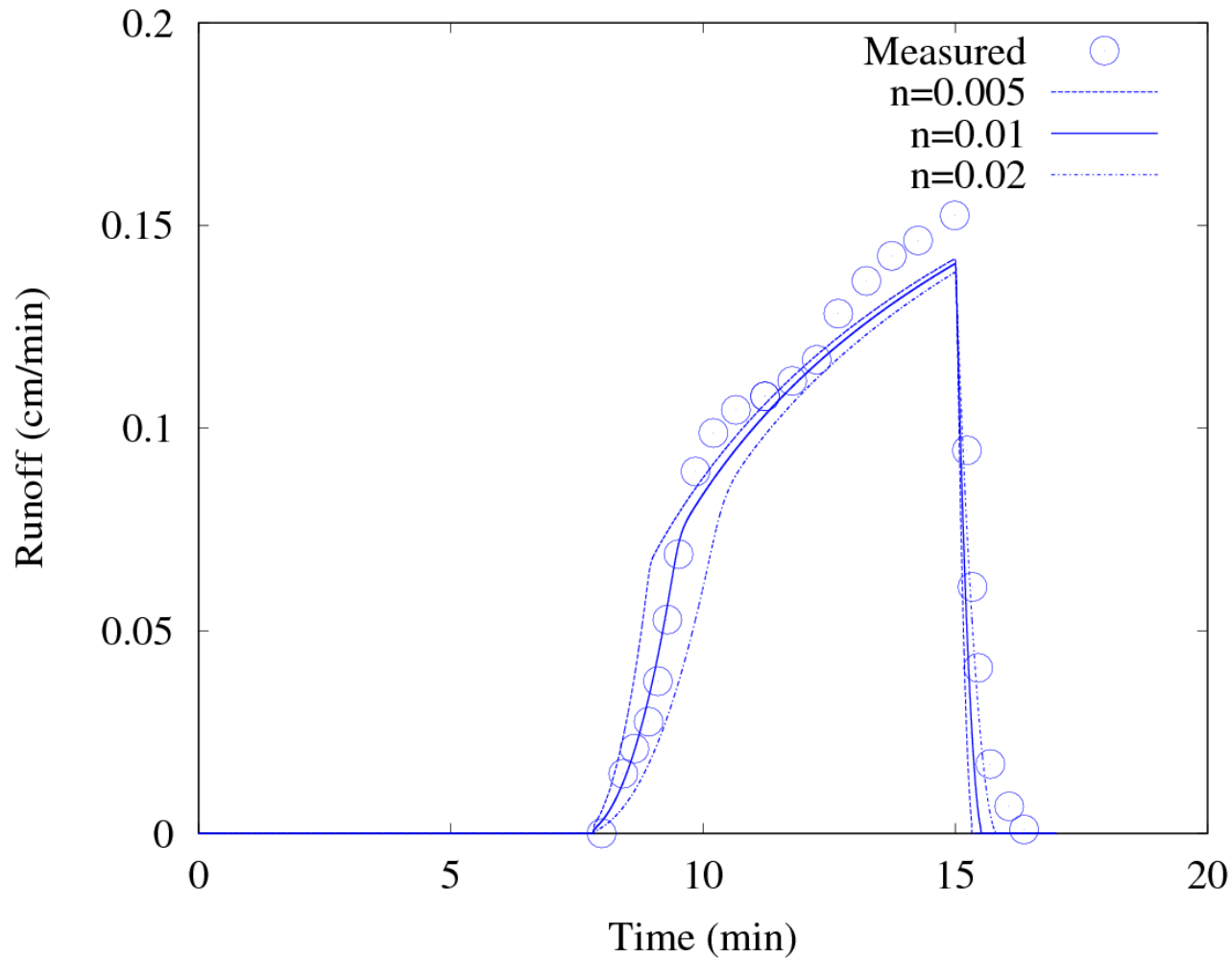
Published laboratory results: sloping plane (Smith and Woolhiser, 1971)

1.22 m deep soil with 3 layers of fine sand with different porosities

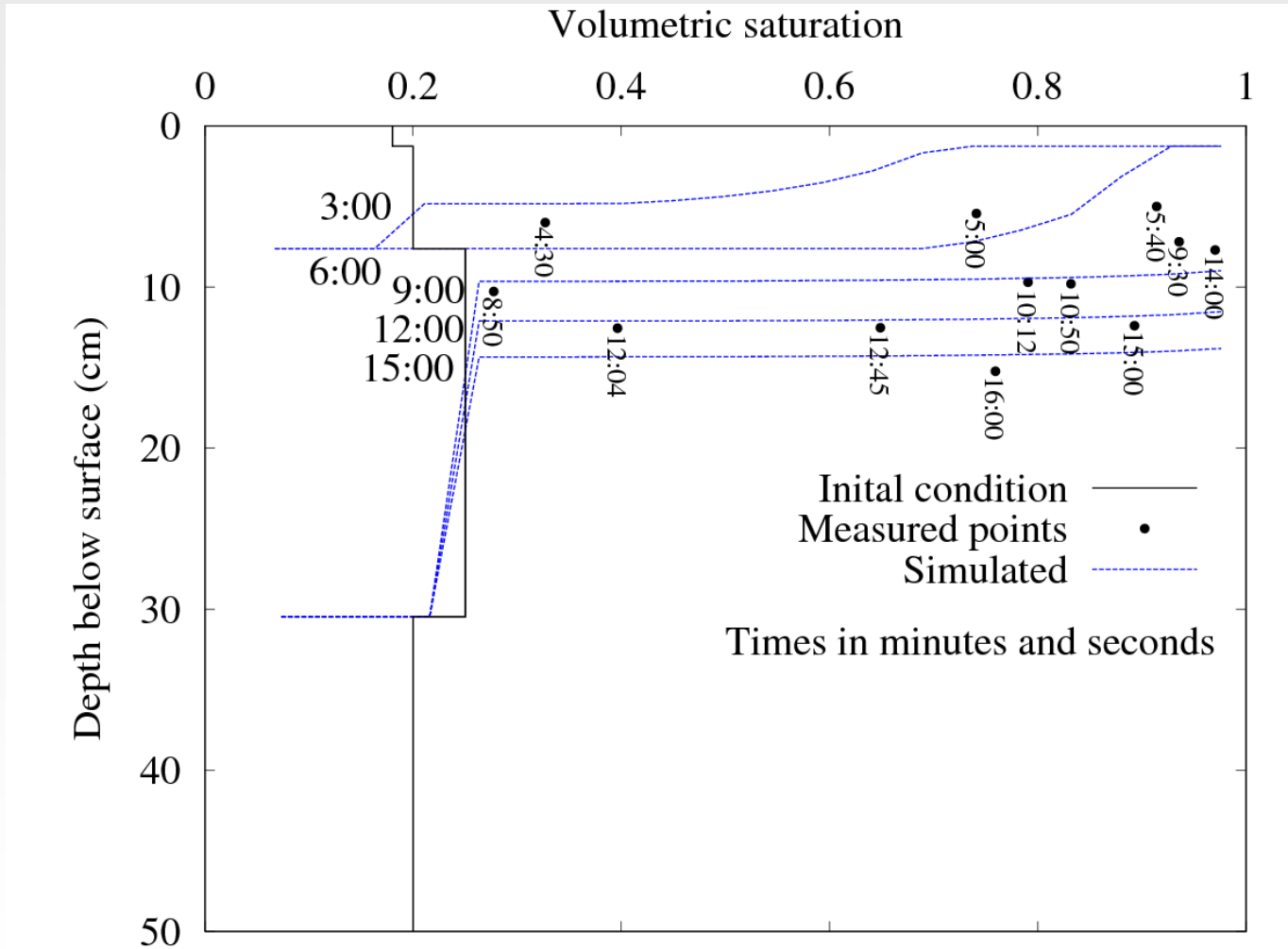
Uniform rainfall intensity of 250 mm/hr for 15 minutes;



Numerical results: Laboratory sloping plane (Smith and Woolhiser, 1971)



Numerical results: Laboratory sloping plane (Smith and Woolhiser, 1971)



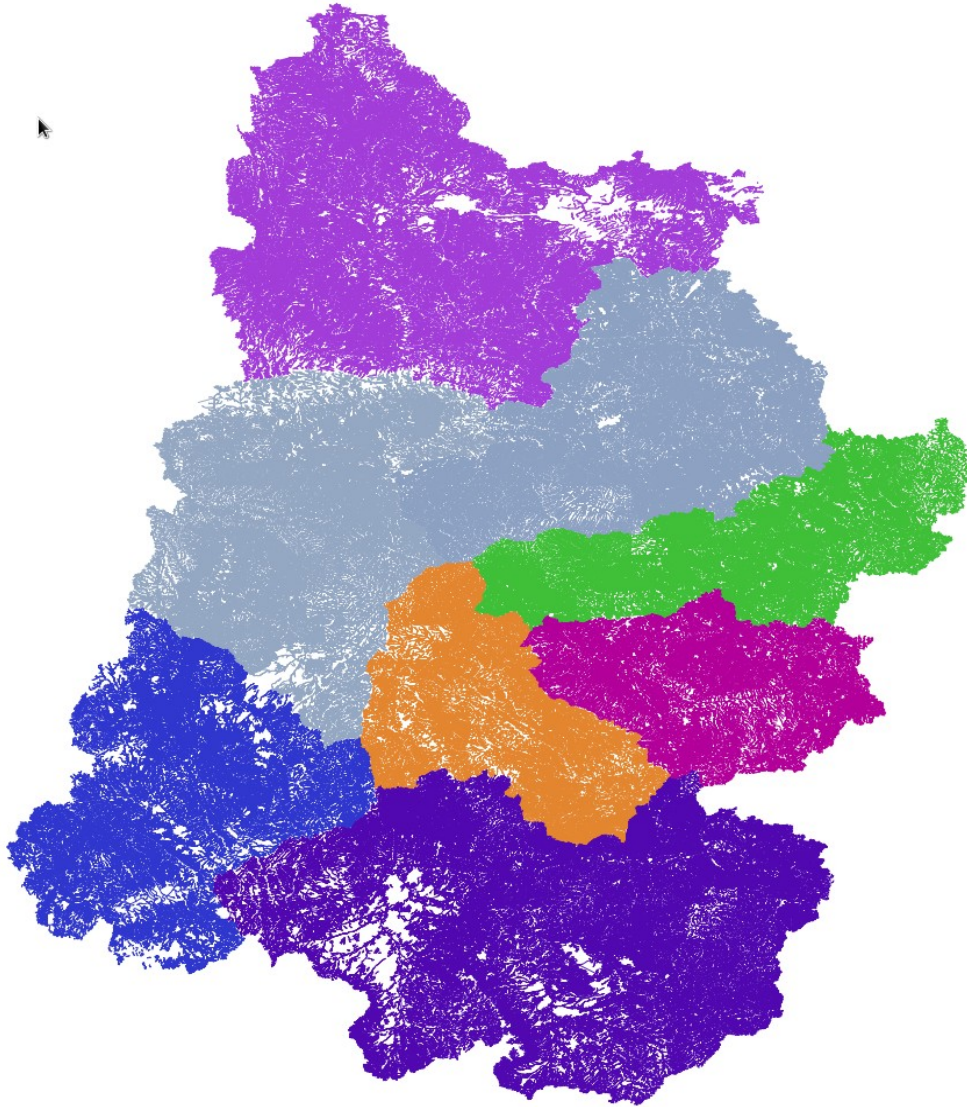
Model Design Philosophy

- Well defined and documented Application Programming Interface (API)
- Written in standard C
- Parallel load balancing by sub-watershed
- Open source (no proprietary code)
- Designed to facilitate addition of alternative process mathematical descriptions

Model Inputs

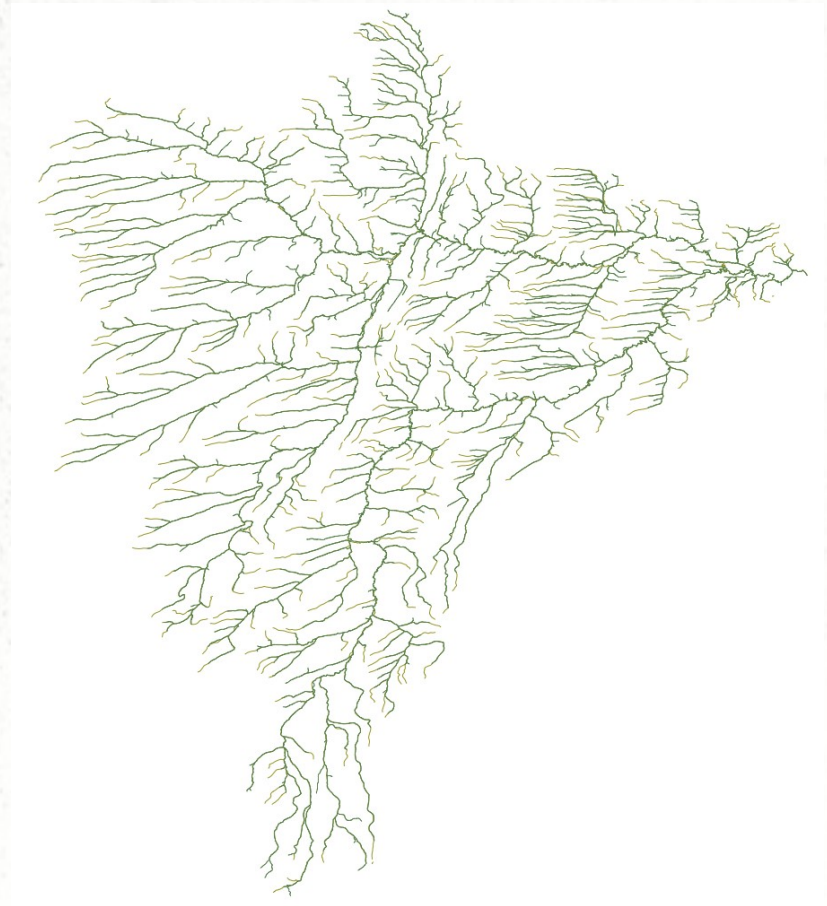
- Topography: USGS NED, SRTM
- Land use/land cover: airborne, satellite or modeled.
- Soils: texture, layers, thicknesses
- Aquifers: alluvial and tributary transmissivity
- Streams: thalweg elevation, cross section, roughness distribution
- Reservoirs, diversions, irrigated areas, water rights
- Forcing: dynamically downscaled climate simulations using Weather Research Forecasting (WRF) model

Upper Colorado River Stream Network



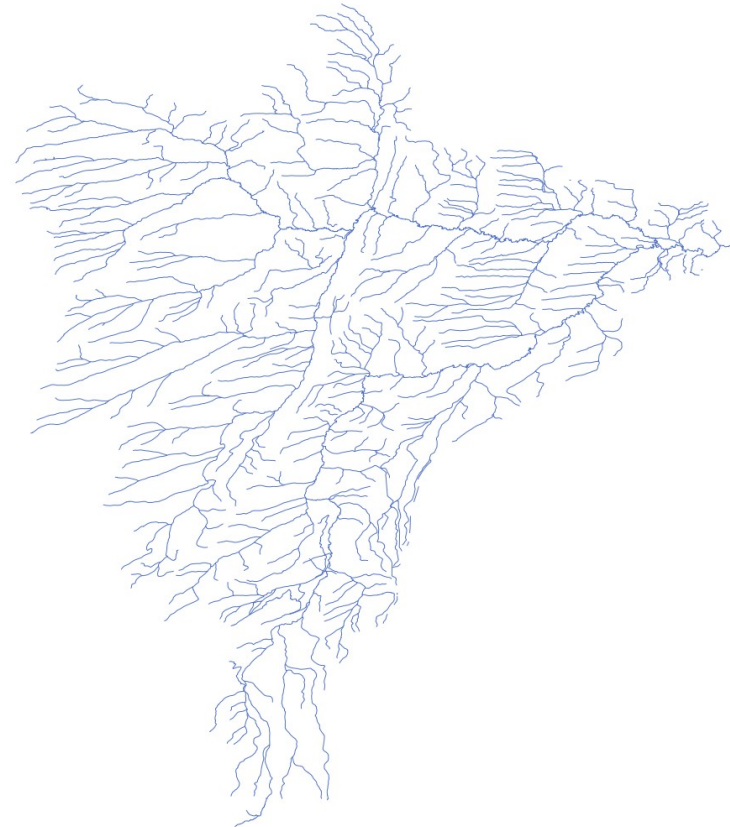
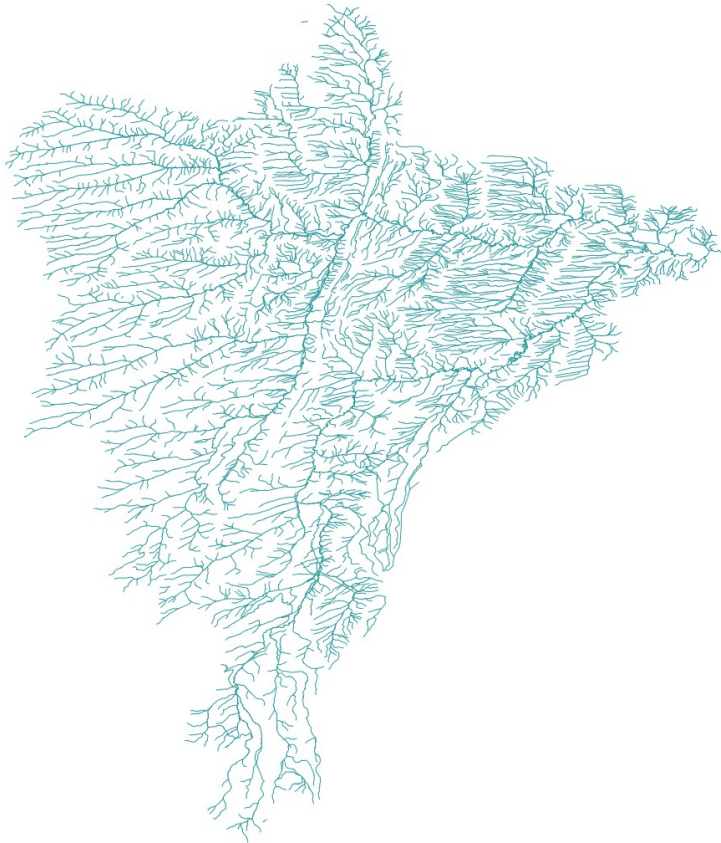
- National Hydrography Data Set (NHD)
- Use geomorphological cross-section predictors
- Almost 500,000 km of streams in NHD
- River data set impossible to create manually

TauDEM vs. NHDPlus



TauDEM Accuracy Assessment

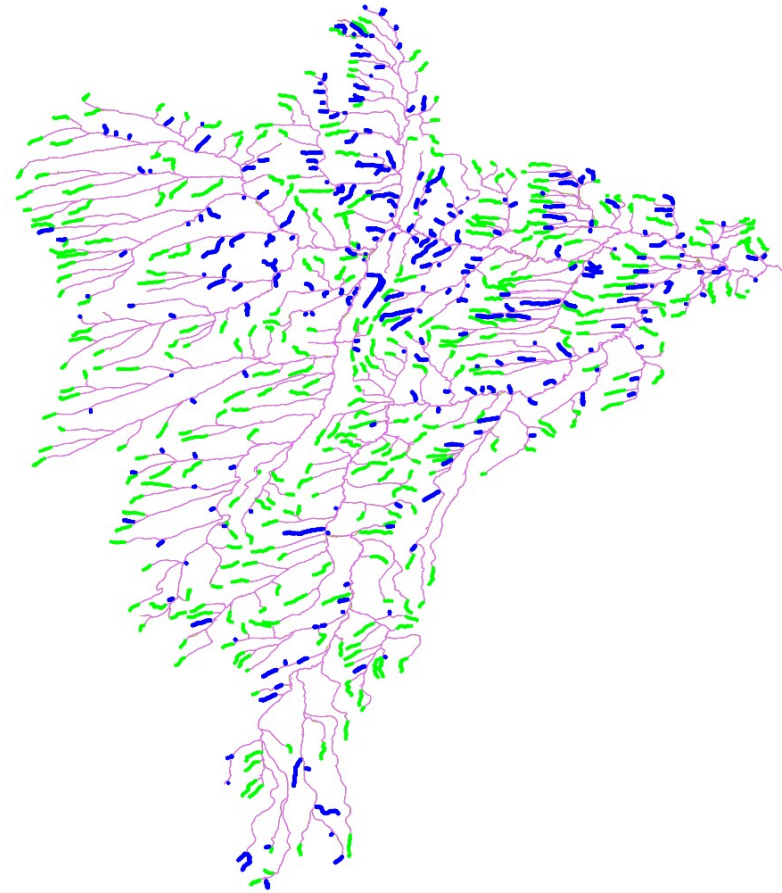
Compared TauDEM generated stream network to
USGS National Hydrography Data Set (NHD)



TauDEM vs. NHDPlus

Picked TauDEM threshold
to match stream density
of NHDPlus

Green and blue lines show
where there is no match
within 100 meters



TauDEM vs. National Hydrography Dataset

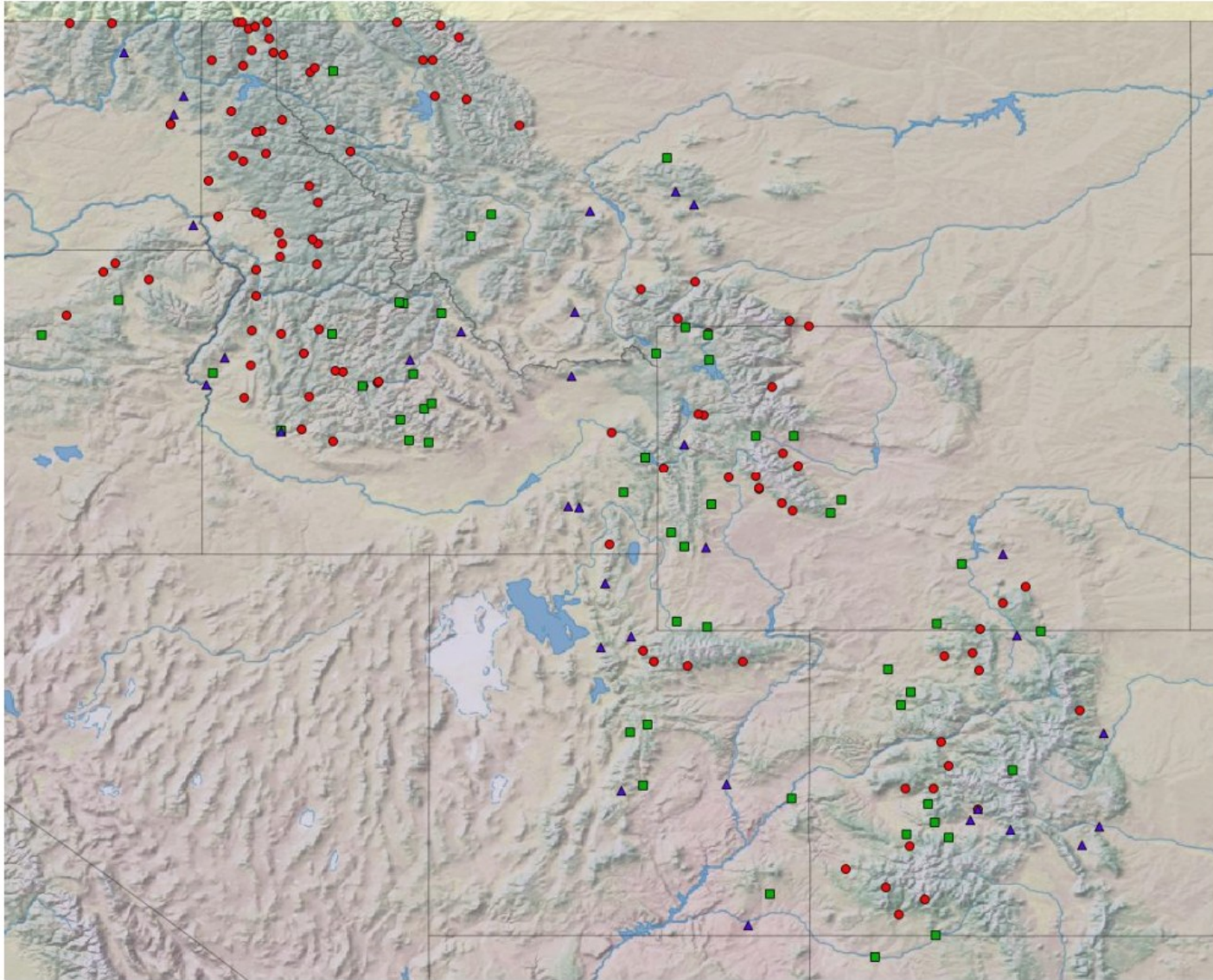
- Qualitatively, TauDEM performs well
- We developed a quantitative algorithm to find points in one set of line segments far away from the closest point in another set of line segments (Hausdorff distance)
- We are submitted a paper describing the algorithm, which will become part of TauDEM

Cross-Section Estimation

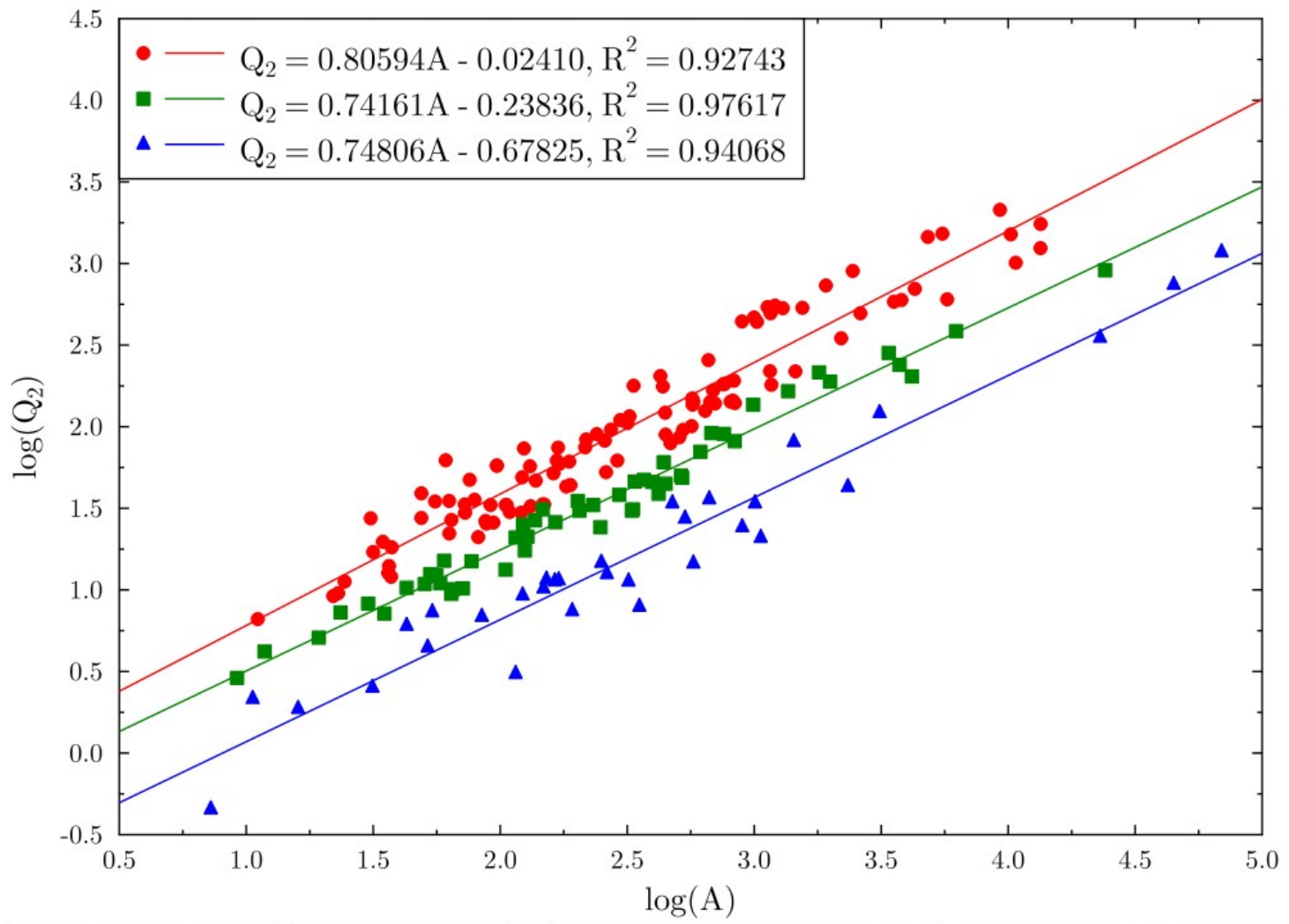
- Channel forming discharge $\sim 2y$ flow
- Tests of simple scaling in Rocky Mountains reveals three populations, all with slope ~ 0.75



USGS Historical Climatological Network



2-year flow



Objectives for next 12 months

- Incorporate lakes, reservoirs, bathymetry in channel network
- Add NOAH-MP evapotranspiration to ADHydro
- Add/test channel routing to ADHydro
- Incorporate Utah Energy Balance and Wyoming Energy Balance snowmelt schemes
- Test ADHydro in Green River headwaters catchment
- Communicate data needs/input structures/work flow to Utah
- Add needed solvers to ADH parallel code and set up partitioner
- Run ADHydro in Parallel on entire Green River in Wyoming, February, 2014
- Release code and establish user community, 2014
- Collaborate with USBR and upper Basin water managers in developing reservoir simulation component.
- Incorporate irrigated areas, begin developing irrigation simulator, summer 2014

Thank you



Establishing a Petascale Collaboratory for the Geosciences: Scientific Frontiers

- “A PCG will enable the simulation of the full spectrum of interactions among physical, chemical, and biological processes in coupled Earth system models.
- Land-atmosphere property fluxes are forced by surface ecosystem heterogeneity on scales of 1 m or less. The forcing is the result of a huge array of interacting biological, chemical, and geological processes
- Understanding the integrated effects of these processes is necessary for predicting ecosystem change and water availability.”

User Interface Toolkit – ezHPC

Tabbed Functions

- MOTD and system news @ HOME Tab
- Monitor Jobs & Queue Status on all machines
- Job Management
 - Script generator & editor
 - Allocation and Utilization viewer
- Fast large file transfers
- Easy access to custom scripts

Monitor Kerberos Ticket Session Time

Easy Access to on-line documentation

The screenshot displays the ezHPC v3.0 web interface. At the top, there's a navigation bar with tabs: Home, Monitor Jobs, Submit Jobs, Manage Files, Manage Scripts, Command Line, Help, and Logout. Below this is a search area with a 'Refresh' button and a note: 'Click 'Refresh' to get a job listing.' The main content area features a tabbed interface with tabs for different machines: BABBAGE, DAVINCI, EINSTEIN, FALCON, HAWK, JADE, MANA, MIDNIGHT, MJM, PINGO, and SAPPHIRE. The 'FALCON' tab is selected. Below the tabs, there are radio buttons for 'My Jobs', 'All Jobs', and 'Other Users' Jobs, and checkboxes for 'Running', 'Pending', and 'Completed'. The primary table lists individual jobs with columns for User ID, Job ID, Status, Wait Time, Start Time, Time Left, End Time, CPUs, Queue, and Sub Project. Below this, a section titled 'Status of Queues on AFRL::FALCON' shows a summary table with columns for Queue, CPUs Running, CPUs Pending, Jobs Running, Jobs Pending, and CPUs Coming Available. A 'Threshold in Hours' is set to 4.

User ID+	Job ID	Status	Wait Time	Start Time	Time Left	End Time	CPUs	Queue	Sub Project
birnbaum	504725	RUN	N/A	Mon Dec 07 1...	00:00:00		2	standard	WPDNRLDC04...
jess	504717	RUN	N/A	Mon Dec 07 1...	00:00:00		24	debug	WPDUSAF349...
johannes	504646	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504660	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504677	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504678	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504679	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504680	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504681	RUN	N/A	Mon Dec 07 1...	00:00:00		24	standard	WPDNRLDC33...
johannes	504682	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504683	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504684	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504685	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504686	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...
johannes	504687	RUN	N/A	Mon Dec 07 1...	00:00:00		30	standard	WPDNRLDC33...

Queue	CPUs Running	CPUs Pending	Jobs Running	Jobs Pending	CPUs Coming Available
background	34	0	3	0	34
debug	24	0	1	0	24
standard	1454	0	54	1	1454
All Queues	1512	0	58	1	1512

HPC Data Issues

- Data assimilation
 - How do we collect enough data to keep a Petascale computer busy? Just inventing data through interpolation is not acceptable.
 - We need a tsunami of data from inexpensive sensors or high-resolution simulations.
 - Satellite images 1-2 times per day in composite (incomplete) JPEG files. This is not necessarily high enough resolution and cloud cover is a problem.
 - *We need a massive number of remote, on ground sensors, not just a massive quantity of data from a relatively few sensors.*
 - We need a symbiotic relationship between smart sensors and computational models, e.g., a dynamic data-driven application system, so that we get the right amount of data for the right scales while computing.
 - Finally, how do we afford massive data collection?

HPC Numerical Algorithms

- Multiscale methods
 - We use a base resolution with an average or median mesh size.
 - We can *upscale* to compute on a coarser mesh much quicker than on the base mesh.
 - We can *downscale* to compute on a finer mesh in a subregion of the entire domain to pick up features that are not visible on the base mesh. If the subregion is small enough, this is both computationally feasible and scientifically useful.
 - Dynamic steering of a computation is essential to make this work and can be done as postprocessing.
- Load balancing
 - This is a preprocessing step in the major computations.
 - First generate base meshes of interest and store them.
 - Generate a series of domain decompositions for different representative numbers of cores and store them.
 - Similar to the ocean modeling community meshes.

HPC Time Stepping

- Implicit methods
 - Implicit time stepping allows larger time steps while maintaining stability.
 - With massively parallel computers, an implicit method requires using massively parallel solvers from one time step to the next, while many common algorithms today just do not scale to $O(100K)$ cores, unfortunately.
- Explicit methods
 - Time steps usually limited by stability conditions to $\Delta t < C(\Delta x)^2$, where C is a positive real constant.
 - A new set of algorithms has recently been developed that are stable on given time steps, but use intermediate time steps (where stability may be violated) so that the stability condition is $\Delta t < C\Delta x$ instead (different C). Hence, vastly larger time steps are possible.
 - Massively parallel computations are straightforward with explicit methods.

HPC Time Stepping

- Hybrid explicit-implicit methods
 - On the boundaries of the subregions use an explicit method to approximate the solution on the next time step.
 - Use an implicit method in each subregion, where the size of the subregions is small enough so that the algorithm used to get to the next time step scales well.
 - Possibly iterate on the boundary points to improve accuracy.
- Hybrid implicit-explicit methods
 - Downscale the problem to only the boundaries of the subregions and use an implicit method to approximate the solution on the next time step. This can be done in parallel based on subregions.
 - Use an explicit method in each subregion.
 - Possibly iterate on the boundary points to improve accuracy.
- Implications for Petascale computing
 - Both hybrid methods should scale and be fast.
 - Need to analyze which hybrid method works best for CI-WATER.